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## Experimentation in a Model-Based Game

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### Abstract

One challenge for building software organisms is to support more autonomous, self-directed learning, rather than induction from annotated data or from blindly explored state spaces. We present a mechanism for learning a simple game given a qualitative model that provides partial information about how actions and quantities influence each other and about tradeoffs among goals. This information lets the learner progressively rule out unproductive actions based on qualitative descriptions of the current situation and to experimentally adjust the relative importance of competing goals. We show that this amounts to operationalizing a qualitative model into a quantitative prescriptive model, which can lead to rapid improvement in performance on a game. In experiments with a simple Human Resources Management game, this approach learned to win after one trial and continued to improve its score and reduce the number of actions needed to win throughout the next nine trials.

### 1. Introduction

Any human-like model of learning should account for the role of prior knowledge. When we learn a new task, we do not start from a blank slate, but, rather, expectations and beliefs guide actions and explanations to permit learning from far fewer trials than is the norm for today's statistical induction methods. We refer to this as *data efficiency*. One way that knowledge can guide learning is through self-directed experimentation in which the learner poses questions to itself and takes actions to winnow down uncertainty and triangulate on ever more accurate models. Knowledge about the domain can help pose questions that refine these models as well as guide the credit assignment process.

Another way to achieve data efficiency is to support a more general notion of state. A learned action policy need not map from concrete primitive states to ground primitive actions, but may comprise abstract states and constraints on them that map to generalized actions. In this way, learning involves a progressive refinement of states and actions that can stop as soon as performance plateaus, rather than exhaustively searching through primitive states. We bring together these ideas with experimentation and reinforcement learning, using prior domain knowledge stated as a qualitative model (Forbus, 2019). We show how such a qualitative model can support self-directed experiments at a high level by exploring quantitative tradeoffs among competing goals. We also show how the same model can guide credit assignment to rule out ineffective action policies. In our approach, qualitative state representations further serve as antecedent conditions on learned action policy rules.

Previous work in active learning and experimentation has focused on supervised learning for classification tasks (e.g., Angluin, 1988) or domain theory acquisition and refinement (e.g., Gil, 1994). These approaches both result in efficient learners, but our alternative differs in the nature of the prior knowledge available to the learner, the necessity for and means of credit assignment, and encoding learned knowledge as an action policy. Research on reinforcement learning has emphasized bottom-up statistical methods that assume no prior knowledge, at the cost of many trials (Sutton & Barto, 2018). Although our mechanism is also unsupervised, it leverages a qualitative domain model to support more efficient learning. We believe this will support a continuum of approaches from highly interactive apprentice-like knowledge acquisition to fully autonomous experimentation.

In this paper, we describe a system that learns to play a simple game given a qualitative model of its mechanics. In the next section, we introduce the domain, the Human Resources Manager game, and its design rationale. In Section 3, we explain how it plays the game using a qualitative model and goal network. Section 4 presents the system’s learning mechanism, including modules for credit assignment, experimentation, experimental controls, and learning goals. Section 5 presents the results from experimental studies of these abilities, Section 6 compares our approach to related research efforts on learning for sequential activity, and Section 7 presents our conclusions and plans for future work.

## 2. The Problem Domain

Human Resources Manager (HRM) is a single-player game in which the objective is to manage a small printing company for 20 months without driving it into bankruptcy or ending with a negative cash flow. The player starts with \$50,000 and a roster of three employees, then makes human resource decisions about hiring, firing, training, promoting, and giving raises to those workers. Unhappy employees quit and former employees sue the company if they were fired improperly. Each of these events has implications for the company’s cash reserves.

HRM was adapted from a 27-year old corporate training simulator (Feifer & Hinrichs, 1992). It is implemented via backchaining rules in a form similar to the Game Description Language (Genesereth & Thielscher, 2014). We chose HRM because it was simple to implement and it has a complex underlying mathematical model, yet it factors out both adversarial and stochastic complexities. Thus, it provides a simple testbed to explore ideas about autonomous experimentation by enabling the system to control quantities and actions. We make no claims for its entertainment or pedagogical value.

Negotiating tradeoffs is key in this setting, as in most strategy games. Finding an effective compromise between competing demands is an abstract task that is a major part of acquiring and refining game strategies. One of our research goals is to discover how to acquire such strategic knowledge with the same basic mechanism as learning action-level policies. There are three main tradeoffs in HRM. First, the goal to reduce labor costs with a low headcount competes with the goal to maximize income. Second, the goal to keep employees happy with high salaries competes with keeping salaries low to reduce labor costs. Third, the goal to invest in employee training competes with keeping payroll costs down. Discovering quantitative compromises for these goals can be viewed as turning a qualitative model into a semi-quantitative model which constrains, rather than optimizes, behavior.

### 3. The Game Player

Before describing our approach to learning, it is helpful to first understand the performance mechanism. In our implementation, the *game player* is a functional part of a Companion agent (Forbus, Klenk & Hinrichs, 2009) that interprets game definition rules and takes random, legal actions. The *learning mechanism* acquires action policies that constrain those choices. Both are built on top of the planning and reasoning facilities provided by the architecture.

To play a game, the player first initializes the game state, which for HRM consists of quantitative properties and relations of the simulated company. On each turn, it queries for legal actions, selects one, and applies it. Most actions take place at the domain level and apply to individual employees, such as giving a raise or evaluating them. These have immediate effects, so we refer to them as *synchronic*. There is a special *diachronic* operator, `doNextTurn`, that advances the simulated time by one month. The player can take any number of actions within a turn and then explicitly advance the time. This happens automatically when there are no more viable actions in a turn. The game is over when the query for a terminal state succeeds, at which point it computes the final score.

The system must learn to select good actions. Instead of starting with a blank slate, like most reinforcement learning agents, it has a qualitative model of the quantities in the game, the graph of their influences, and the qualitative effects of actions on quantities. For example, giving an employee a raise increases their salary, which in turn positively influences the employee’s attitude and the company’s labor costs. The learning problem is to figure out how to balance these competing factors and identify conditions for taking actions.

The qualitative model for HRM was manually constructed by abstracting the quantitative equations in the game’s rules. Prior work has shown the feasibility of learning a qualitative model from demonstration (Hinrichs & Forbus, 2012), but this was not the current research focus. The HRM model has 37 reified quantity types and 53 influences linking quantities, actions, and events. A quantity type may be instantiated for each employee or for the company itself.

Because the qualitative model ultimately connects intermediate quantities like salary to the top-level game goal, it is possible to automatically translate the quantity influences into subgoals. A static analysis routine walks the qualitative influences starting from the root goal quantities and reifies goals, as described in Hinrichs and Forbus (2016). Here, the goal types that are produced are all of the form ‘maximize (or minimize) some quantity type’. As a side effect of building this goal network, static analysis detects tradeoffs by identifying quantity types that both positively and negatively influence the same quantity. Figure 1 shows the goal network for HRM, where the oval nodes indicate goals with direct tradeoffs.

We refer to a goal in this goal network as *operational* if there is a qualitative influence between some primitive action and the goal quantity. For instance, maximizing an employee’s salary is operational because there is a qualitative dependence of employee salary on the action `doGiveRaise`. Higher-level goals, such as maximizing employees’ attitudes, may be active but are not operational because there is no direct control over attitudes.

The reified goal network serves an additional purpose of keeping track of the relative *activations* of goals throughout the game. These roughly correspond to each goal’s importance and thereby the proportional allocation of effort expended in pursuing it. Conceptually, if the top goal to win the game has 100 percent activation, then that activation is subdivided among its subgoals. By default, activation is allocated evenly, so that it serves as an informal proxy for importance relative to the top-level goal. Activation will be set to zero, however, if a goal type has no entities to which it applies. For example, a goal to maximize employee salaries will be inactive if there are no em-

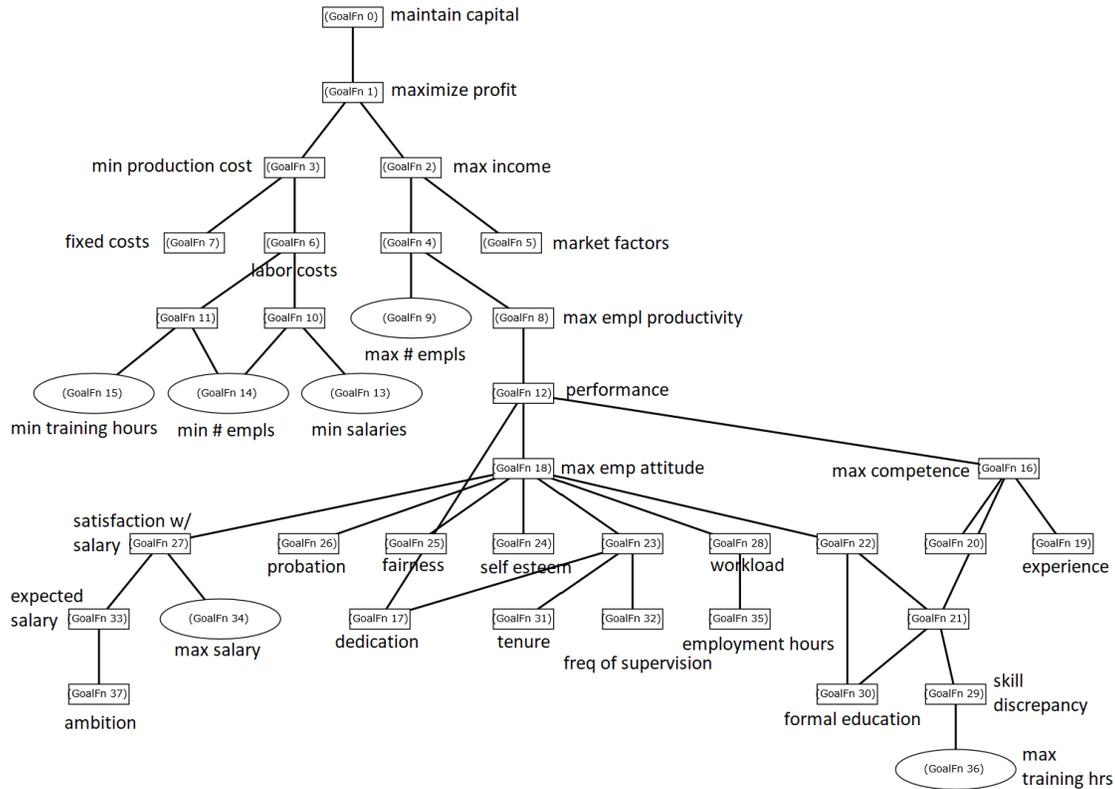


Figure 1. Goal network for HRM computed from the qualitative model.

ployees. Also, goal activation can be explicitly set by a meta-level planning action. This is how experimentation sets a tradeoff balance when exploring tradeoffs.

The effect of goal activation is to control the likelihood of picking actions that serve one goal over another. For goals that are pertinent to a single entity, such as the company, this results in stochastically picking an action or not, by simply using the goal activation percentage as the selection threshold. If the activation is 80%, then it will take that action roughly 80% of the time and take a competing action the other 20%. For goals that apply to many entities, activation serves to divide actions by entity. For example, if the goal of maximizing salaries is 20%, then only one fifth of employees should receive raises. We refer to this as an *action budget* for a type-level goal. The action budget ensures that no single action type monopolizes the available resources.

The next stage of action selection is to further constrain candidate actions by consulting any learned action policies or experimental conditions. Initially, there are no policies, so behavior appears goal-directed but still somewhat random. An action policy provides bounds on when an action should or should not be performed. This is encoded in declarative statements of the form (<cc-type> <learning goal> <condition-name> <action-spec>)

where

<cc-type> = controlCondition | controlConditionLowerBound | controlConditionUpperBound

<action-spec> = (<directive> <generalized-action>)

<directive> = ruleIn | ruleOut .

Table 1. Procedure for action selection with a qualitative model and an action policy.

```

foreach domain goal in decreasing order of activation do
  while meets_action_budget(goal)
    legal ← legal_actions(goal)
    acceptable ← filter_by_action_policy(legal)
    action ← instantiate_with_most_underperforming_entity(acceptable)
    Take action
    Record before/after quantity changes
    Refine action policy
  end
end

```

Here, a *learning goal* names the explicit reified goal to learn when to apply the action. Learning goals are posted by the learning mechanism in response to performance failures and other expectation failures. A *condition name* is a functional term that specifies an inequality between quantity fluents. A *generalized action* is a primitive action, some of whose arguments may have been lifted to typed variables. For example, (`doHRMPromote gameEmployee`) is the generalized action of promoting someone, as opposed to a particular employee.

When action policies exist for the candidate actions, the game player queries the inequality in the named condition to determine if the condition is active and, based on whether it is a lower bound or upper bound, it adopts the directive (or its opposite, respectively), to accept or reject the action. A simple control condition that is neither an upper nor lower bound is an experimental control that is used to force the selection or rejection of a particular action in order to explore the state space or to suppress confounding behaviors. Note that the named condition inequality defines a qualitative state, but that state definition may contain constant numeric thresholds. Thus, as it acquires and refines action policies, its knowledge can become increasingly quantitative.

The pseudocode in Table 1 summarizes the action selection process. When the game player chooses an action to take, it steps through active, operational domain goals in decreasing order of activation. The system identifies action predicates that influence the goal quantity and queries for ground legal actions. If there are action policies or experimental conditions on the action predicate, it filters the actions and selects the action whose entity argument is underperforming the most with respect to the goal. For example, only the most underpaid employees should receive raises. Finally, it takes the action in the game and records the quantity changes as it computes the next state.

#### 4. Learning Mechanism

Our primary objective is to devise a learning mechanism that acquires abstract lessons autonomously from as few trials as possible. To this end, experimentation helps to *curate* experience by strategically guiding exploration, while credit assignment extracts powerful lessons from each trial. Supporting both of these is a qualitative model that guides both activities. What is learned are action policy rules that allow or prohibit an action based on a qualitative description of the game state. These rules are refined progressively with experience, both immediately after taking an action and

retrospectively after an event signifying a failure (typically game loss). In both cases, the qualitative model guides the identification of salient quantities whose values create or refine the initial qualitative state description. Thus, the inputs to the learning mechanism are sampled quantity values identified by credit assignment in response to significant events, such as losing the game, and the outputs are action policies that constrain behavior.

#### 4.1 Credit Assignment

Part of data-efficient learning is drawing powerful or general conclusions from each trial. Credit assignment seeks to explain the underlying cause of a failure by reasoning about the chain of qualitative influences from an action to a manifestation of failure. When the player loses a game, it carries out a *post-mortem* analysis. It looks back in time to the most recent action that led to the loss. In general, this is an arbitrarily hard problem, but the qualitative model provides strong guidance in reconstructing the causal trail back to poor decisions.

Post-mortem analysis examines the current situation to identify the quantities contributing to the loss. For HRM, this is the company's capital (cash reserves) reaching zero. It then traces backward in time, looking for a change in the profit rate until it reaches the turn in which some action must have influenced the company's capital. It searches the indirect (i.e., synchronic) influences on capital until it finds an action that negatively impacted the profit rate, such as giving a raise or firing somebody. The post mortem uses the results of credit assignment to post learning goals to determine the conditions under which the action primitive should or should not be applied, creates or refines the action policy for that action, augments the set of quantities to be recorded for future credit assignment, and schedules follow-up experiments to further refine the policy.

Another kind of credit assignment happens during the game, when the result of an action does not have the expected effect on downstream, high-level quantities. This does not mean that the action was incorrectly described but, rather, that in the particular quantitative state under which the action occurred, it affected multiple quantities that combined to reduce the overall performance. For example, firing a good employee might reduce labor costs, but it might decrease income even more. This immediate credit assignment need not walk back through time, since it already knows which action was invoked. The routine identifies salient quantities as those whose value changed when the action was taken and caused the undesirable quantity change downstream. With this information, it refines the action policy for the action using the same mechanism as post-mortem credit assignment.

#### 4.2 Generalization

To prevent the same mistake from being made in similar circumstances, the agent constructs a policy for that action which may initially be extremely specific to the particular action and situation, but is progressively refined and generalized as new examples are encountered. Whereas an action policy in most reinforcement learners maps directly from states to utilities, our learner instead acquires and generalizes *constraints* on actions. In particular, an action policy rule conditions an action specification with a qualitative state. The action specification either requires or prohibits an action, which may itself be lifted or generalized. For example, a policy might prohibit promoting AmbitiousAlice when her performance is less than 20 and her attitude is less than 50. Such a rule would look like

```
(controlConditionLowerBound
  (LearnCondForActionFn doHRMPromote)
  (MostSpecificConditionFn doHRMPromote)
  (ruleOut (doHRMPromote AmbitiousAlice)))
```

where first argument is the learning goal, the second argument is a functional term denoting the name of a model fragment that defines a qualitative state, and the third term is the action specification. The model fragment, in turn, relates the quantity conditions

```
(and (< (performance AmbitiousAlice) 20)
      (< (attitude AmbitiousAlice) 50)).1
```

As new failure or success instances are encountered, the ranges on quantities are extended and the arguments to the action specifications are lifted as necessary. We adapted this representation to support experimental controls and it has the additional benefit of being relatively concise and explainable to humans.

### 4.3 Autonomous Experimentation

Autonomous or self-directed experimentation is the process by which the learner proposes and executes experiments to reduce its uncertainty about the domain. There are two reasons for such experimentation: to strategically curate experience and to simplify credit assignment. Our system addresses the former by systematically varying experimental parameters and the latter by controlling other exogenous parameters to restrict possible causes of change. In addition, it organizes experiments around explicit declarative learning goals as a way to be strategic about the exploration process. These learning goals are posted by the credit assignment mechanism and specify two different kinds of manipulation: *action experiments* and *tradeoff experiments*.

An action experiment is created when a postmortem traces a failure to an action that either directly caused a game loss or caused a trend that ultimately led to the loss. The agent posts a learning goal to refine the conditions under which the action is advisable. It then schedules experiments to refine the conditions by exploring the region between the most specific state to rule out and the most general. In other words, it reduces the uncertainty by driving the qualitative state conditions in a manner similar to candidate elimination in the version-space framework (Mitchell, Utgoff, & Banerjee, 1980).

Tradeoff experiments, on the other hand, attempt to explore higher-level decisions by controlling the relative activations of competing goals. For example, if the baseline allocations of activation for competing goals are evenly divided, then a tradeoff learning goal will spawn two experimental trials, emphasizing first one goal and then the other by setting its activation to 75 percent vs. 25 percent. Subsequent experiments further extrapolate or interpolate the best performing allocation so far. These tradeoff experiments go even further toward simplifying credit assignment by suppressing all actions that cannot influence either of the competing goals. Consequently, this tradeoff identification mechanism can be thought of as off-policy learning. Because tradeoff studies manipulate a single independent parameter (the ratio of two goal activations), no credit assignment is needed at all and it identifies the best quantitative tradeoff by hill climbing based on the game score. One caveat is that this assumes tradeoffs themselves are independent of each other.

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<sup>1</sup> We have simplified the syntax here for the purposes of presentation.

## 5. Empirical Evaluation

To evaluate our approach to learning game expertise, we ran trials under the two conditions, action learning and tradeoff learning. A trial here, also known as an “epoch” in the reinforcement learning literature, is one complete game. We first tested action learning by having the system play autonomously through pure trial and error while honoring the goals and qualitative model. Our hypothesis was that the goal network would suggest plausible actions to take and the accumulation of action policy constraints would further refine the conditions under which they were attempted, yielding incremental performance improvement beyond merely surviving twenty turns. We measured the operating capital of the simulated company at the end of the last turn. In these trials, the agent learned to rule out actions that failed to have an immediate benefit as predicted by the qualitative model. It also learned from post-mortem analysis to rule out actions that had a long-term negative effect leading to a loss of the game.

Initially, performance was spectacularly bad. Because every action in the game serves some goal, it micromanaged and tried to pursue every action as often as possible. In some cases, it tried firing everybody in the first few turns, leaving the fixed costs to drive the company into bankruptcy shortly afterward. Figure 2 shows the results of the first three trials and the tenth trial. Each chart shows the progression of the company-wide capital, income, and production cost over time. While the first trial ended with bankruptcy in turn 5, by the second trial it had learned an action policy that ruled out firing employees in most conditions and had discovered that hiring more employees was the key to surviving past turn 20. In trials 3 through 10, the system continued to improve the final outcome by increasing the profitability of the company until it banked \$240,000 by turn 20 in the tenth trial. This bore out our expectation that performance would continue to improve even after it learned to win the game.

In addition to the performance curves, the charts also present the actual sequence of actions and events that occurred in the trial. We can see from this that the system quickly stopped firing employees and learned to hire earlier in the game. Moreover, as it refined the action policies, the agent learned to play with a lighter touch so that by trial 10, it achieved better performance with far fewer actions that consisted of hiring additional employees, giving a few raises and evaluations, one promotion, and one training course. Thus, although the qualitative goal network suggests that every action serves some goal, the gradual refinement of action policy adds quantitative constraints on when it is effective to take those actions. To be clear, this is a very simple, deterministic game and the objective is not especially difficult to achieve. In fact, under the baseline conditions of taking no actions at all, the company only fails after 19 turns. However, the point of these experiments was to show how quickly the learner improves given fairly minimal background knowledge.

The second study examined tradeoff learning. Our hypothesis was that qualitative goal tradeoffs can provide a small number of parameters that can be explored, resulting in global improvements in behavior. Our metric was the same as for the action learning trials. Figures 3 and 4 show the results. Here, because tradeoffs can be enumerated ahead of time, the system scheduled an initial set of six trials to extrapolate tradeoff ratios in either direction from the baseline tradeoff allocation. In the first two trials, the agent explored the salary tradeoff by first setting the activation of the goal to minimize salaries at 50 percent vs. 0 percent for maximizing salaries. Of course, since there is no action to reduce salaries, both activations imply never giving a raise. Moreover, since all other actions are suppressed, Trial 1 is equivalent to the baseline condition of taking no actions at all. Note that because this policy uses no learned knowledge, it is an offline policy.

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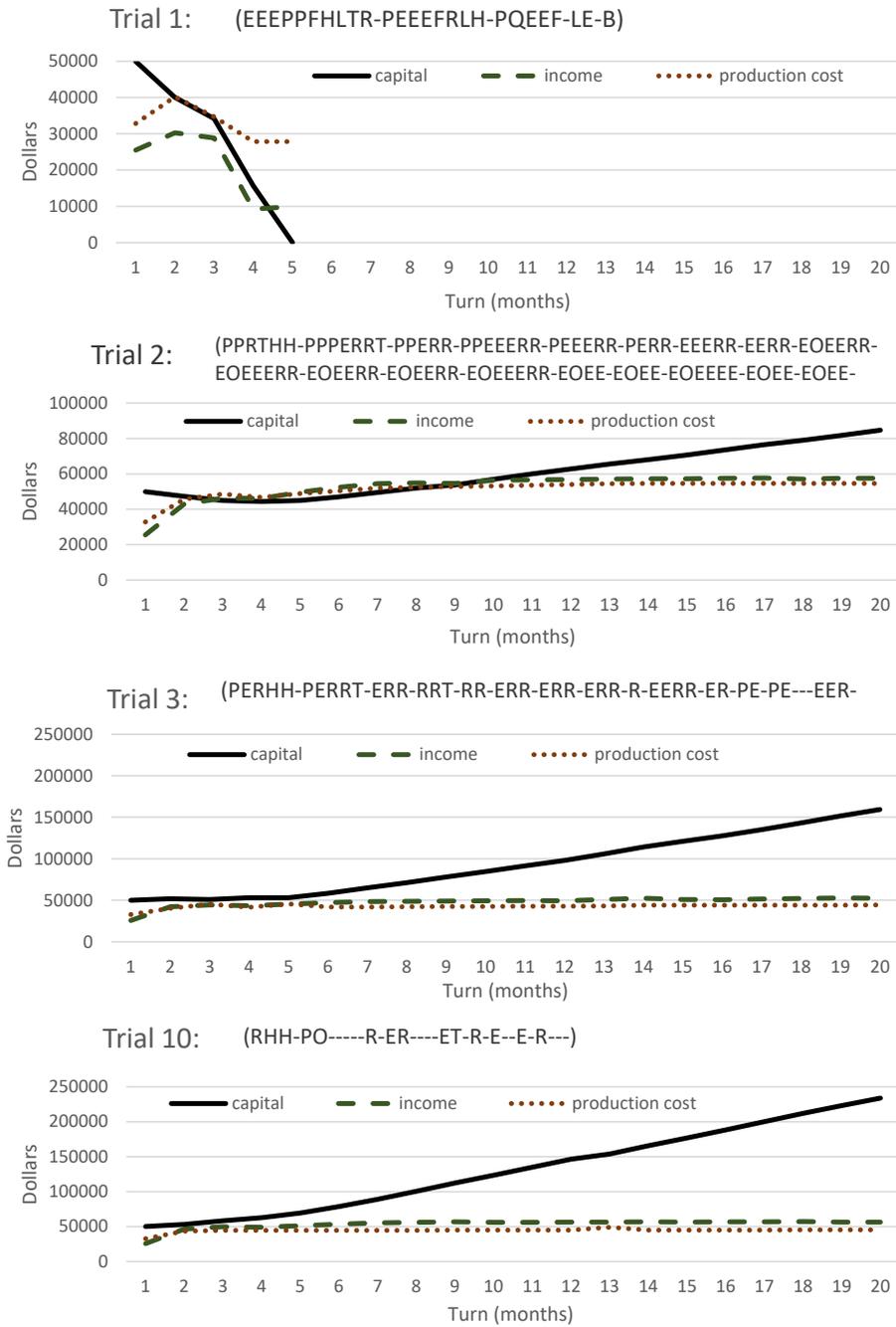


Figure 2. Action learning trials 1, 2, 3 and 10. The action abbreviation key is: Evaluate, Promote, Hire, Fire, Raise, Train, Lawsuit, Overpaying, and Bankruptcy. A dash signifies the next turn operation.

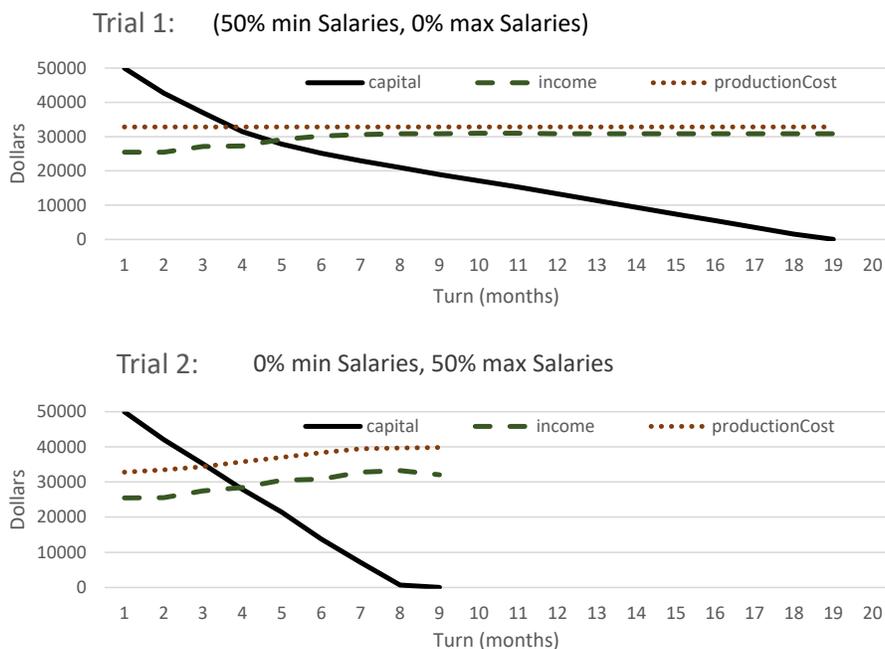


Figure 3. In tradeoff learning trials 1 and 2, the system explored the tradeoff between minimizing salaries to reduce labor costs and maximizing salaries to increase attitude and productivity.

After this, the agent explored the tradeoff between reducing labor costs by omitting training (Trial 3) and increasing employee competence by training employees (Trial 4). As with the salary dimension, there is no ‘untrain’ action, so by not training anyone and suppressing all other actions, Trial 3 is equivalent to the baseline condition. Trial 4 did train an employee in the first turn, but the only evidence was a small spike in production cost, causing it to lose two turns earlier than in the baseline condition. In the final pair of trials, the agent explored the tradeoff between having fewer employees to reduce labor costs (Trial 5) and having more employees to increase production (Trial 6). The effect of reducing head count by firing approximately half the staff was swift and severe: labor costs dropped, but fixed costs stayed the same causing profits to nosedive, leading to bankruptcy in turn 6. Finally, in Trial 6, by hiring two additional employees at the beginning of the game, income (barely) exceeded production cost and the company remained profitable.

Because the tradeoff experiments suppressed all actions that were unrelated to the goal tradeoff, they were essentially *off-policy* learning (i.e., they did not exploit prior learning). Consequently, the trials do not form a learning curve and the final results would have been the same if performed in any order. The purpose of imposing such experimental controls was to eliminate confounding factors that could hinder accurately determining the better tradeoff ratio. Ultimately, the tradeoff trials merely suggest one way for a learning agent to experiment at a more abstract level than primitive operators. As currently implemented, the relative goal activations of competing goals are a coarse mechanism for controlling behavior and further refinement of the tradeoff ratios would not appreciably improve performance in this domain. Despite this, the system learned to win the game in six trials, which is data efficient by most standards.

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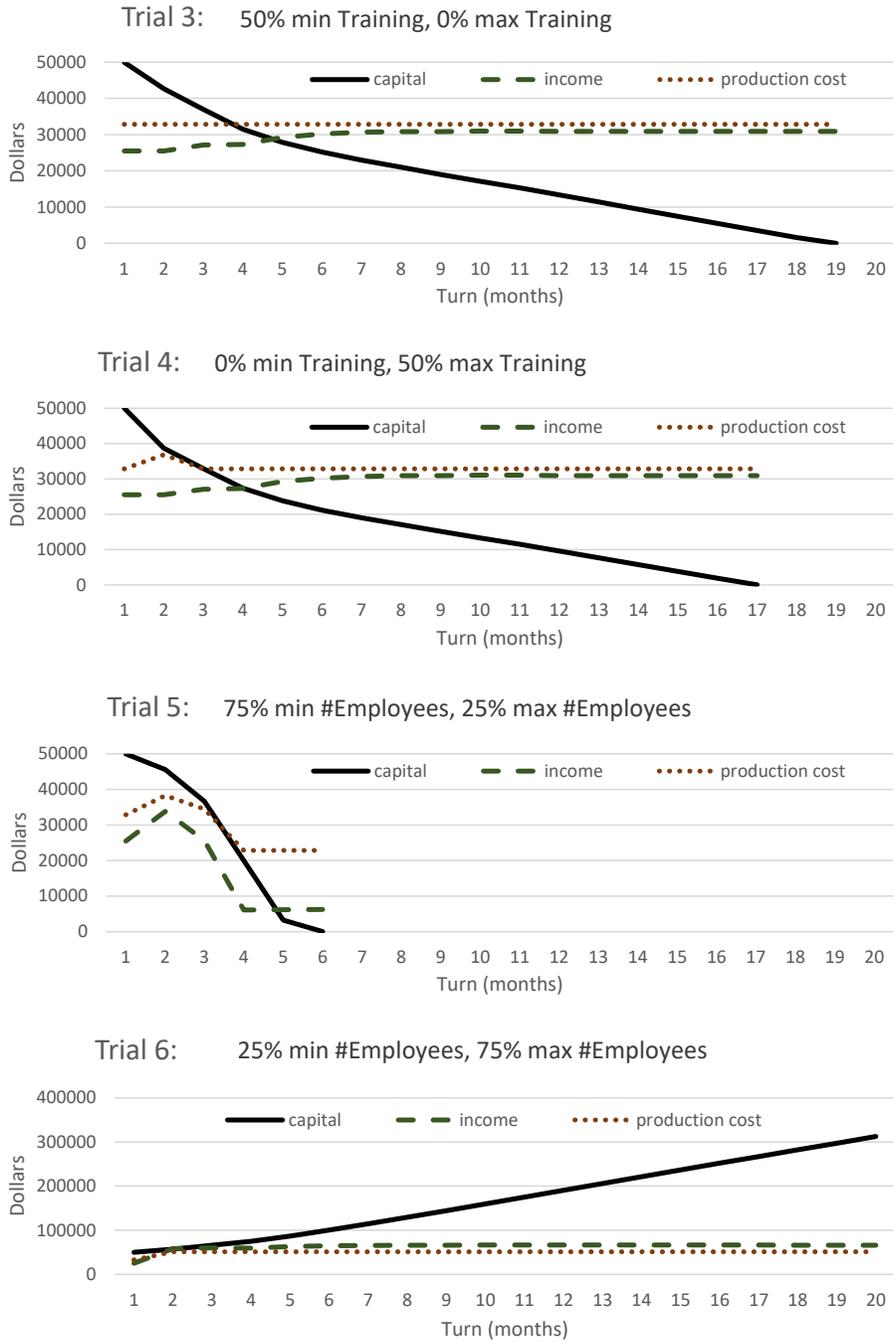


Figure 4. In tradeoff learning trials 3 and 4, the system explored the effect of training on performance. In trials 5 and 6, it explored the tradeoff between minimizing the number of employees to reduce labor costs and maximizing the number of employees to increase productivity.

## 6. Related Work

The approach described in the previous section derives from ideas in several areas, most notably automated experimentation and active learning, reinforcement learning, and qualitative modeling. The main driver has been the desire for an agent that designs its own experiments and pursues its own learning goals in ways that make use of available domain knowledge. This builds on prior work in *active learning* and *experimentation*. The primary difference is that active learning assumes a semi-supervised task in which an agent judiciously chooses queries to pose to an oracle to quickly learn to classify instances (Settles, 2012). Like active learning, our approach emphasizes data-efficient induction that uses prior knowledge to identify and prioritize gaps. Our mechanism for action policy learning has some precedent in hypothesis refinement as version space search (Mitchell, 1977). Unlike active learning, we focus on unsupervised acquisition of tactical or strategic behavior in game playing, rather than on classification.

Experimentation is a more fully autonomous, unsupervised form of learning in which the agent designs and runs experiments to validate or refute its own hypotheses. Part of this involves imposing experimental controls to minimize conflating factors and simplify credit assignment. Important early work in experimentation addressed operator refinement and acquired domain knowledge about operator applicability (e.g., Gil, 1994). Experimentation identified and revised missing conditions and effects of planning operators that led to anomalous outcomes in execution. In a similar way, our system schedules and runs experiments to refine the conditions under which an operator should be applied. Unlike operator refinement, we are concerned less with repairing incomplete domain theories and are focused more on learning the advisability of different actions in different situations to improve behavior. We use a qualitative domain model to guide credit assignment and to encode experimental controls. In addition, the model fragments used to specify operator applicability are easily decomposed into sets of inequalities that effectively turn experimental design into a search through a parametric space. In our approach, an experiment generalizes or specializes a quantity condition while holding other conditions fixed.

More recent work tends to blur the distinction between active learning and experimentation, (e.g., Wang, Garrett, Kaelbling, & Lozano-Pérez, 2018; Konidaris, Kaelbling, & Lozano-Perez, 2018). This focuses on model and representation learning rather than classification and involves active sampling of the environment rather than querying of an expert oracle. The objective in these efforts is to learn a model or symbolic representation from perceptual data that supports planning. Because the learning agents are physical robots, data-efficient learning is critically important. At a high level, our approach is similar, except that our learner starts with a symbolic, qualitative model and learns to improve its performance on an abstract game. The point of our experiments is to better understand the benefits of this initial knowledge endowment for learning.

Reinforcement learning is another paradigm from which we have borrowed liberally. This varies along several dimensions, including whether it is model free or model based, whether states are discrete or continuous, how and when exploration is carried out, what kind of reward or punishment is provided, how it accounts for delayed effects, and whether actions are hierarchical. The technique we have presented here is clearly a variant of model-based learning, which enables the application of planning by referencing content about the system’s dynamics (Botvinick & Weinstein, 2014). Typically, these are quantitative models defined in terms of differential equations or neural networks. Our approach is definitely model based, because it learns the quantitative effects of taking particular actions in particular states, but it differs in the nature of the model, which is a set of qualitative influences.

Historically, continuous-state reinforcement learning has been addressed through function approximation, which requires careful selection of a basis, such as a CMAC (Santamaría, Sutton, & Ram, 1997) or radial basis function (Santos, 1999). In our work, qualitative models are used to discretize the continuous space. In fact, the entire point of qualitative models is to carve up a continuous space into semantically or causally meaningful phases. This has the benefit of being concise and communicable through language.

Although it is generally considered to be a form of unsupervised learning, Sutton and Barto (2018) claim that reinforcement learning is orthogonal to the supervised-unsupervised distinction. Instead, they argue that it is the exploration-exploitation tradeoff that largely defines the paradigm. Work in this area has focused on finding near-optimal mechanisms for determining *when* to explore new states vs. exploit learned knowledge (e.g., Kearns & Singh, 2002; Brafman & Tenenholz, 2002). We have focused instead on knowledge-directed experimentation that determines *what* to explore. In other words, most reinforcement learners treat exploration as random selection of actions or states that have not been previously encountered. In our approach, exploration amounts to experimental design that strategically extrapolates or interpolates quantity conditions on when to use an action. It pursues reified learning goals and varies experimental conditions to minimize random exploration.

The nature of feedback in our system is more punitive than reinforcing. This is because the qualitative model implicitly provides initial rewards in the form of the goal hierarchy. There is no need to search blindly for actions that might positively influence the top-level goal. Instead, it learns to suppress actions when they are contraindicated by the particular quantitative state. Delayed effects in reinforcement learning are handled through a variety of methods, including eligibility traces (Singh & Sutton, 1996) and temporal differences (Sutton, 1988). Our approach to handling such effects is the model-based mechanism for credit assignment described in Section 4. This shares some aspects of model-free mechanisms, but benefits from prior knowledge of the game dynamics.

Reinforcement learning typically requires hundreds to thousands of trials to learn even simple behaviors because it exhaustively explores the state space of the system. Hierarchical decomposition is one technique for mitigating scaling problems due to high dimensionality by exploiting temporal abstraction (Barto & Mahadevan, 2003). It would be interesting to see if the game player’s goal network supports the sort of stratified control found in such hierarchical systems. Another way that reinforcement learning deals with the explosion of states, especially when actions or states take on continuous values, is through function approximation. Our use of qualitative states to encode action policies can be viewed as a knowledge-derived variant of this technique. This is a necessity for the HRM domain, which has 37 quantity fluent types, nine of them company wide and 29 being employee parameters. Given seven possible employees, this totals 212 concrete continuous quantity fluents, most of which can take on values from 0 to 100. Naïvely encoding states by partitioning the continuous quantities into buckets would be computationally prohibitive.

AlphaGo and its successor AlphaGoZero are well known as successful reinforcement learners (Silver et al., 2016; Silver et al., 2017). They achieved superhuman performance in playing Go after millions of trials of self play, starting from what its developers claimed to be a blank slate. Although extremely impressive, this is almost the exact opposite of our objective. Our approach purposely exploits prior knowledge in order to achieve acceptable performance on a game with very few trials. We believe that prior knowledge is not something to exorcise from a learner, but rather that it plays an important role in efficient learning. Marcus (2018) goes farther in arguing for the importance of *innate* knowledge in his analysis of AlphaZero and the game knowledge that is inevitably built in to the learner.

More generally, the issue of data efficiency has been addressed in other forms of learning. Transfer seeks to accelerate learning in one task or domain by reusing learned knowledge (such as facts, biases, features, or subplans) acquired from another task or domain (Pan & Yang, 2009; Konidaris, Scheidwasser, & Barto, 2012). One-shot learning (e.g., Li, Fergus, & Perona, 2006) primarily focuses on object recognition and achieves data efficiency through expertise transferred from prior learning on other categories, reducing the incremental cost of learning to recognize a new category. Zero-shot learning seeks to master a task (typically recognition) with no prior training examples of the target (Xian, Schiele, & Akata, 2017) by leveraging prior learning on other objects and features extracted from word embeddings. The mechanism we present does not involve classification learning and does not transfer from a different task, but rather builds on a symbolic representation of a qualitative model. If the model were acquired by learning from demonstration or instruction, then it could be considered a type of transfer. Model acquisition is beyond the scope of this paper, but Hinrichs and Forbus (2012) provide an example.

Behavioral cloning is a method for learning by imitation that is often applied to learning to control a dynamic system (Michie, 1993; Bratko & Suc, 2003; Torabi, Warnell, & Stone, 2018). Our approach of using a qualitative model to guide learning and carve up a continuous space is especially similar to Bratko and Suc’s (2003) approach, although the current system learns through experimentation rather than imitation. Our approach to the credit assignment problem bears some similarity to Langley’s (1985) strategy learning program SAGE. This refined the conditions for applying legal operators by comparing differences between their successful and unsuccessful applications. A key difference is that our use of a qualitative domain model guides credit assignment by making causal relationships explicit, and it traces back in time to earlier states by following direct influences.

## 7. Conclusions

A qualitative model is one kind of prior knowledge that can guide learning. Such a model takes the form of a set of declarative structures that can aid induction and support performance. One role is to facilitate experimentation, which reduces ambiguity in credit assignment by imposing controls on what to vary and what to hold constant. We have presented two ways to achieve this aim: generalizing or specializing qualitative state conditions on action selection and manipulating the tradeoff ratios of activations for competing goals. In both cases, the result is to operationalize the qualitative model by learning quantitative policies for pursuing actions or goals.

A major property of the learning technique described here is data efficiency. The approach attains good performance in under ten trials by starting with a qualitative domain model and ruling out portions of the potential search space whenever an action fails to provide a performance benefit predicted by the model. The learner need not wait until the end of the game to receive an extrinsic reward, since the model and its derived goal network provide immediate feedback via an audit trail from any action through intermediate quantities to the top-level goal. We believe that the resulting data efficiency is an important property of any learning system that purports to behave in a manner remotely like humans.

We designed the HRM game to be a simple testbed for exploring experimentation. The next step is to apply the capabilities described here in Freeciv (<http://freeciv.wikia.com>), a much more difficult strategy game. We predict that self-directed experimentation will let a Companion (Forbus, Klenk, & Hinrichs, 2009) learn continuously, over weeks and months, with minimal human intervention. It remains to be seen whether such learning will scale, run afoul of the utility problem (Minton, 1988), or otherwise become unstable. We believe that prior knowledge, afforded by an

extensive repository of qualitative domain models, will mitigate these problems, as will natural language advice provided by a human mentor (McFate, Forbus, & Hinrichs, 2014).

We are also developing an intermediate-level representation for tactics so that experimentation can explore how and when to apply larger units of behavior than primitive actions. Another avenue for future work will be treating learning goals more like domain goals, with their own activations, measurable properties, explicit processes, and strategies. This may ultimately permit further improvement by revising the order of experiments and conditions for stopping. This would be a further step toward developing software organisms that not only behave independently but also learn independently.

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